BiPartite Graph:

A graph having cycle of odd length will not be bipartite.  
Two adjacent nodes can’t have same color in bi partite graph.

A graph having cycle of even length will be bipartite and also without cycle.

Hint -> Dividing a graph resembles Bi Partite Graph Problem